





TRAIL: Near-Optimal Imitation Learning with Suboptimal Data

Sherry Yang

Sergey Levine Ofir Nachum







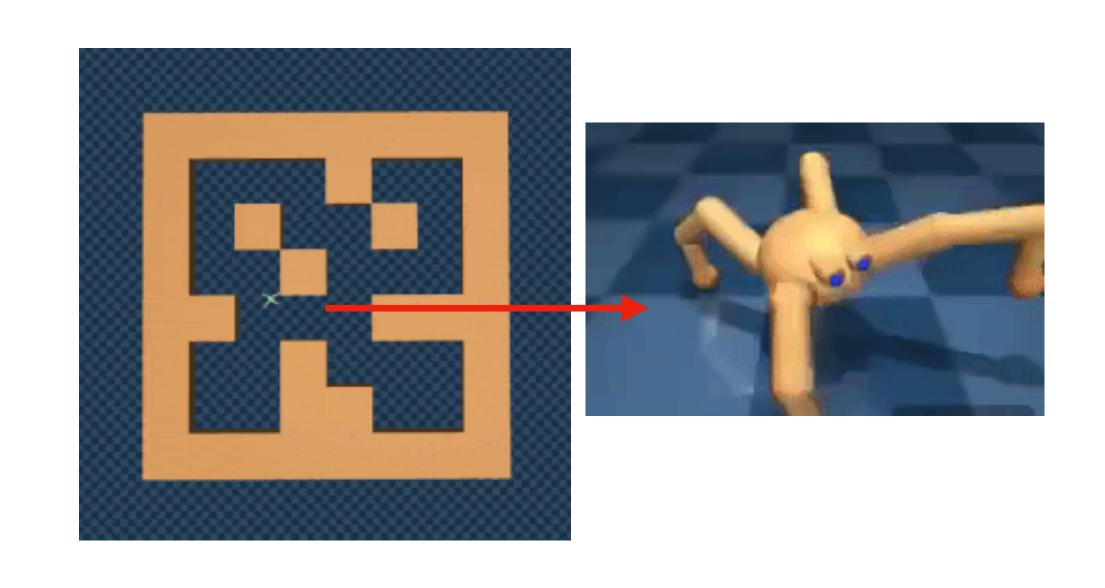
Paper: https://openreview.net/pdf?id=6q_2b6u0BnJ

Code: https://github.com/google-research/google-research/tree/master/rl_repr

Imitation Learning

Given expert demonstrations \mathcal{D}^{π^*}

Learn π that recovers π^* : Diff $(\pi, \pi_*) = D_{\mathrm{TV}}(d^{\pi} || d_*^{\pi})$



Behavioral cloning:

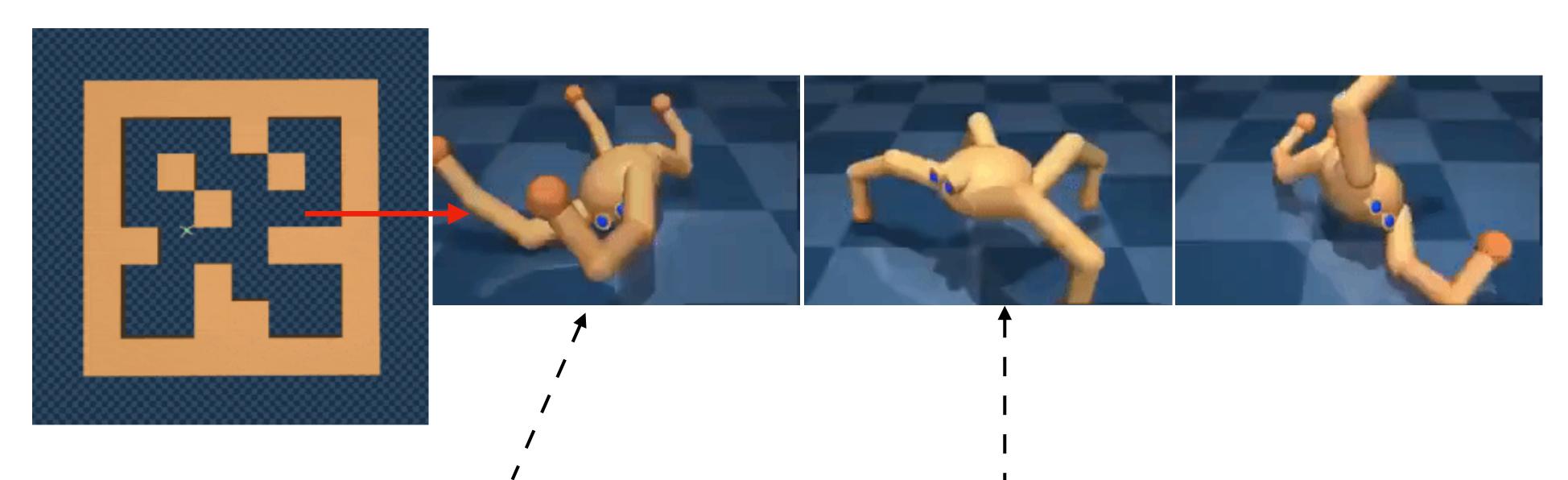
$$J_{\text{BC}}(\pi) := \mathbb{E}_{(s,a) \sim (d^{\pi_*},\pi_*)} [-\log \pi(a|s)]$$

Limited & Hard to obtain (e.g., involves human expert)

Suboptimal Offline Data

Large amounts of suboptimal offline data \mathcal{D}^{off}

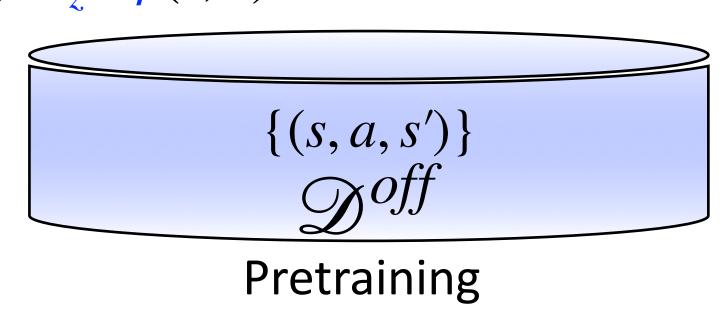
How can \mathcal{D}^{off} provably facilitate imitation learning?



- Highly suboptimal (e.g., random policy)
- Single modal (e.g., collected by <u>one</u> stationary policy)

Factored transition model





$$Pretraining \begin{cases} \underbrace{\mathbb{E}_{(s,a)\sim d^{\mathrm{off}}}\left[D_{\mathrm{KL}}(\mathcal{T}(s,a)\|\mathcal{T}_{Z}(s,\phi(s,a)))\right]}_{=J_{\mathrm{T}}(\mathcal{T}_{Z},\phi)} \end{cases} \tag{1}$$

Action decoder

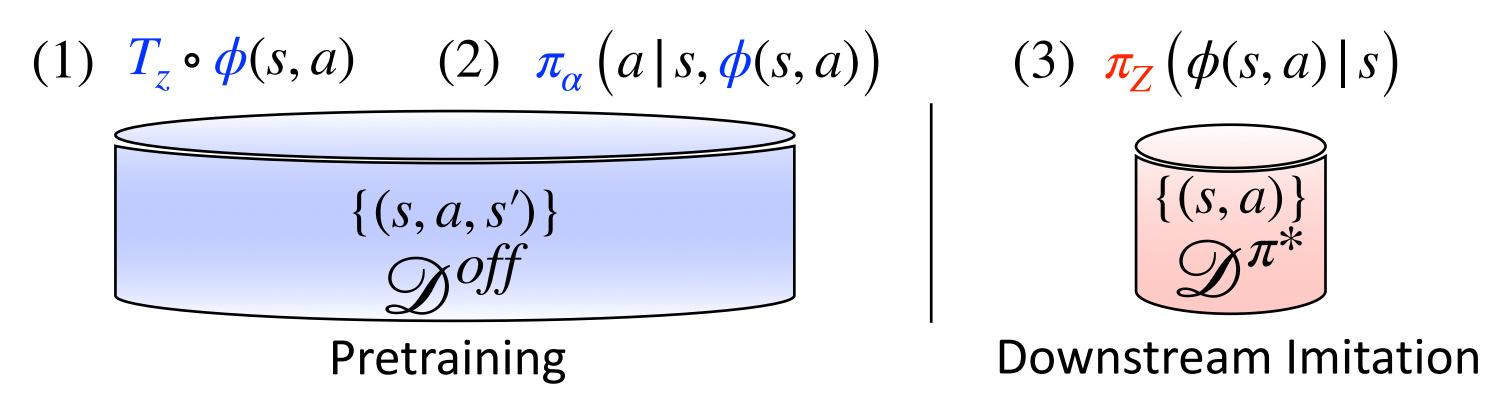
(1)
$$T_z \circ \phi(s, a)$$
 (2) $\pi_\alpha \left(a \mid s, \phi(s, a) \right)$

$$\{(s, a, s')\}$$

$$\text{Off}$$
Pretraining

Pretraining
$$\begin{bmatrix} \mathbb{E}_{(s,a) \sim d^{\text{off}}} \left[D_{\text{KL}}(\mathcal{T}(s,a) \| \mathcal{T}_{Z}(s,\phi(s,a))) \right] \\ = J_{\text{T}}(\mathcal{T}_{Z},\phi) \\ \mathbb{E}_{s \sim d^{\text{off}}} \left[\max_{z \in Z} D_{\text{KL}}(\pi_{\alpha^{*}}(s,z) \| \pi_{\alpha}(s,z)) \right] \\ \approx \operatorname{const}(d^{\text{off}},\phi) + J_{\text{DE}}(\pi_{\alpha},\phi) \end{cases}$$
(1)

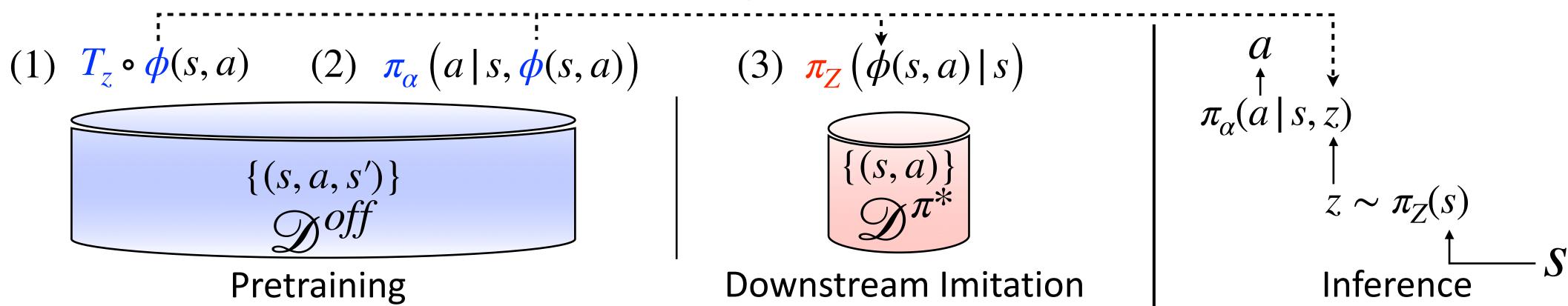
Latent policy



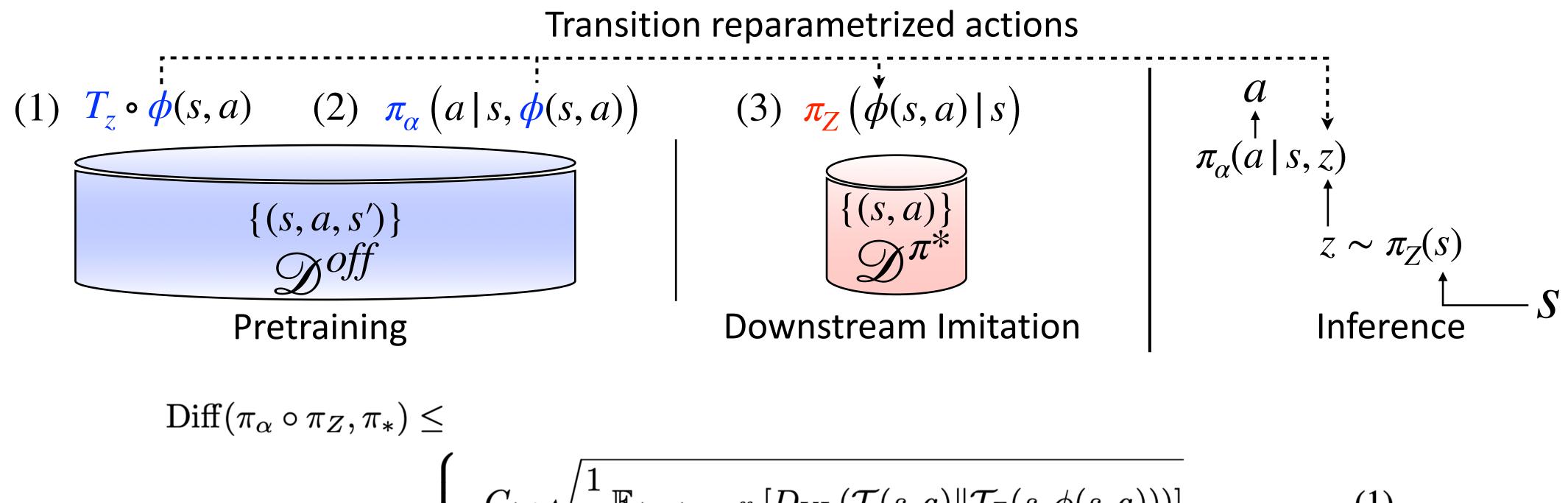
$$\begin{cases}
\mathbb{E}_{(s,a)\sim d^{\text{off}}} \left[D_{\text{KL}}(\mathcal{T}(s,a) \| \mathcal{T}_{Z}(s,\phi(s,a))) \right] \\
= J_{\text{T}}(\mathcal{T}_{Z},\phi) \\
\mathbb{E}_{s\sim d^{\text{off}}} \left[\max_{z\in Z} D_{\text{KL}}(\pi_{\alpha^{*}}(s,z) \| \pi_{\alpha}(s,z)) \right] \\
\approx \operatorname{const}(d^{\text{off}},\phi) + J_{\text{DE}}(\pi_{\alpha},\phi)
\end{cases}$$

$$\begin{array}{c}
\mathbb{E}_{s\sim d^{\pi_{*}}} \left[D_{\text{KL}}(\pi_{*,Z}(s) \| \pi_{Z}(s)) \right], \\
\mathbb{E}_{s\sim d^{\pi_{*}}} \left[D_{\text{KL}}(\pi_{*,Z}(s) \| \pi_{Z}(s)) \right], \\
= \operatorname{const}(\pi_{*},\phi) + J_{\text{BC},\phi}(\pi_{Z})
\end{cases}$$
(3)

Transition reparametrized actions



$$Pretraining \begin{cases} & \underbrace{\mathbb{E}_{(s,a)\sim d^{\mathrm{off}}}\left[D_{\mathrm{KL}}(\mathcal{T}(s,a)\|\mathcal{T}_{Z}(s,\phi(s,a)))\right]}_{=J_{\mathrm{T}}(\mathcal{T}_{Z},\phi)} & \\ & \underbrace{\mathbb{E}_{s\sim d^{\mathrm{off}}}\left[\max_{z\in Z}D_{\mathrm{KL}}(\pi_{\alpha^{*}}(s,z)\|\pi_{\alpha}(s,z))\right]}_{z\in Z} & \\ & \approx \mathrm{const}(d^{\mathrm{off}},\phi) + J_{\mathrm{DE}}(\pi_{\alpha},\phi) & \\ \\ Downstream \\ & \underbrace{\mathbb{E}_{s\sim d^{\pi_{*}}}\left[D_{\mathrm{KL}}(\pi_{*,Z}(s)\|\pi_{Z}(s))\right],}_{=\mathrm{const}(\pi_{*},\phi) + J_{\mathrm{BC},\phi}(\pi_{Z})} & (3) \end{cases}$$



$$Pretraining \begin{cases} C_{1} \cdot \sqrt{\frac{1}{2}} \underbrace{\mathbb{E}_{(s,a) \sim d^{\text{off}}} \left[D_{\text{KL}}(\mathcal{T}(s,a) \| \mathcal{T}_{Z}(s,\phi(s,a))) \right]}_{= J_{\text{T}}(\mathcal{T}_{Z},\phi)} \\ + C_{2} \cdot \sqrt{\frac{1}{2}} \underbrace{\mathbb{E}_{s \sim d^{\text{off}}} \left[\max_{z \in Z} D_{\text{KL}}(\pi_{\alpha^{*}}(s,z) \| \pi_{\alpha}(s,z)) \right]}_{\approx \text{ const}(d^{\text{off}},\phi) + J_{\text{DE}}(\pi_{\alpha},\phi)} \\ = \text{const}(\pi^{*},\phi) + J_{\text{DE}}(\pi^{*},\phi) \\ = \text{const}(\pi^{*},\phi) + J_{\text{BC},\phi}(\pi_{Z}) \end{cases}$$

$$C_{1} = \gamma |A|(1-\gamma)^{-1}(1+D_{\chi^{2}}(d^{\pi_{*}} \| d^{\text{off}})^{\frac{1}{2}}) |C_{2}|_{C_{2}} = \gamma(1-\gamma)^{-1}(1+D_{\chi^{2}}(d^{\pi_{*}} \| d^{\text{off}})^{\frac{1}{2}}) |C_{3}|_{C_{3}} = \gamma(1-\gamma)^{-1} \end{cases}$$

Sample Complexity of TRAIL

$$\mathbb{E}_{\mathcal{D}^{\pi_*}}[\text{Diff}(\pi_{opt,Z}, \pi_*)] \le (1)(\phi_{opt}) + (2)(\phi_{opt}) + C_3 \cdot \sqrt{\frac{|Z||S|}{n}}$$

So far, our analysis is based on tabular latent actions.

What about continuous latent actions and stochastic expert policy?

TRAIL with Linear Transition Dynamics

$$\begin{aligned} & \text{deterministic} & \text{linear: } T_z = w(s')^\top \phi(s, a) \\ & \text{Diff}(\pi_\alpha \circ \pi_\theta, \pi_*) \leq (1)(T_Z, \phi) + (2)(\pi_\alpha, \phi) \\ & Downstream \\ & Imitation \end{aligned} \left\{ + C_4 \cdot \left\| \frac{\partial}{\partial \theta} \mathbb{E}_{s \sim d^{\pi_*}, a \sim \pi_*(s)} [(\theta_s - \phi(s, a))^2] \right\|_1 \end{aligned} \right.$$

TRAIL with Linear Transition Dynamics

$$\begin{aligned} & \text{deterministic} & \text{linear: } T_z = w(s')^\top \phi(s, a) \\ & \text{Diff}(\pi_\alpha \circ \pi_\theta, \pi_*) \leq (1) (\mathcal{T}_Z, \phi) + (2) (\pi_\alpha, \phi) \\ & & Downstream \\ & Imitation \end{aligned} \left\{ + C_4 \cdot \left\| \frac{\partial}{\partial \theta} \mathbb{E}_{s \sim d^{\pi_*}, a \sim \pi_*(s)} [(\theta_s - \phi(s, a))^2] \right\|_1 \right\}$$

easier to optimize compared to:

$$C_3 \cdot \sqrt{\frac{1}{2}} \underbrace{\mathbb{E}_{s \sim d^{\pi_*}} [D_{\mathrm{KL}}(\pi_{*,Z}(s) || \pi_Z(s))]}_{= \mathrm{const}(\pi_*, \phi) + J_{\mathrm{BC}, \phi}(\pi_Z)}$$

Learning TRAIL in Practice

(1)
$$T_z \circ \phi(s, a)$$

$$\begin{aligned} \text{TRAIL EBM: } &\mathcal{T}_Z(s'|s,\phi(s,a)) \propto \rho(s') \text{exp}(-\|\phi(s,a)-\psi(s')\|^2) \\ &\mathbb{E}_{d^{\text{off}}}[-\log \mathcal{T}_Z(s'|s,\phi(s,a)))] = \text{const}(d^{\text{off}}) + \frac{1}{2} \mathbb{E}_{d^{\text{off}}}[\|\phi(s,a)-\psi(s')\|^2] \quad \text{contrastive learning} \\ &+ \log \mathbb{E}_{\tilde{s}'\sim \rho}[\text{exp}\{-\frac{1}{2}\|\phi(s,a)-\psi(\tilde{s}')\|^2\}] \end{aligned}$$

Learning TRAIL in Practice

$$(1) \quad T_z \circ \phi(s, a)$$

TRAIL EBM:
$$\mathcal{T}_Z(s'|s,\phi(s,a)) \propto \rho(s') \exp(-\|\phi(s,a)-\psi(s')\|^2)$$
.
$$\mathbb{E}_{d^{\mathrm{off}}}[-\log \mathcal{T}_Z(s'|s,\phi(s,a)))] = \mathrm{const}(d^{\mathrm{off}}) + \frac{1}{2}\mathbb{E}_{d^{\mathrm{off}}}[\|\phi(s,a)-\psi(s')\|^2] \quad \text{contrastive learning} \\ + \log \mathbb{E}_{\tilde{s}'\sim \rho}[\exp\{-\frac{1}{2}\|\phi(s,a)-\psi(\tilde{s}')\|^2\}]$$

TRAIL linear: $\overline{\mathcal{T}}(s'|s,a) \propto \rho(s') \exp\{-||f(s,a) - g(s')||^2/2\} \propto \overline{\psi}(s')^{\top} \overline{\phi}(s,a)$

recover $ar{\phi}$ with random Fourier features: $ar{\phi}(s,a) = \cos(Wf(s,a) + b)$

Learning TRAIL in Practice

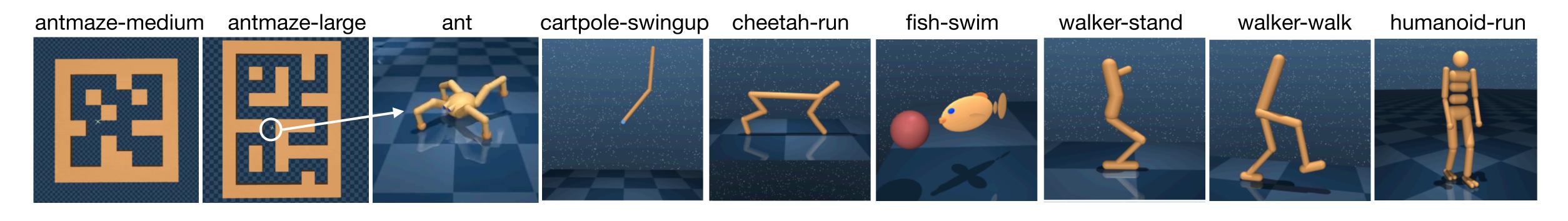
$$(1) \quad T_z \circ \phi(s, a) \qquad (2) \quad \pi_\alpha \left(a \mid s, \phi(s, a) \right) \qquad (3) \quad \pi_Z \left(\phi(s, a) \mid s \right)$$

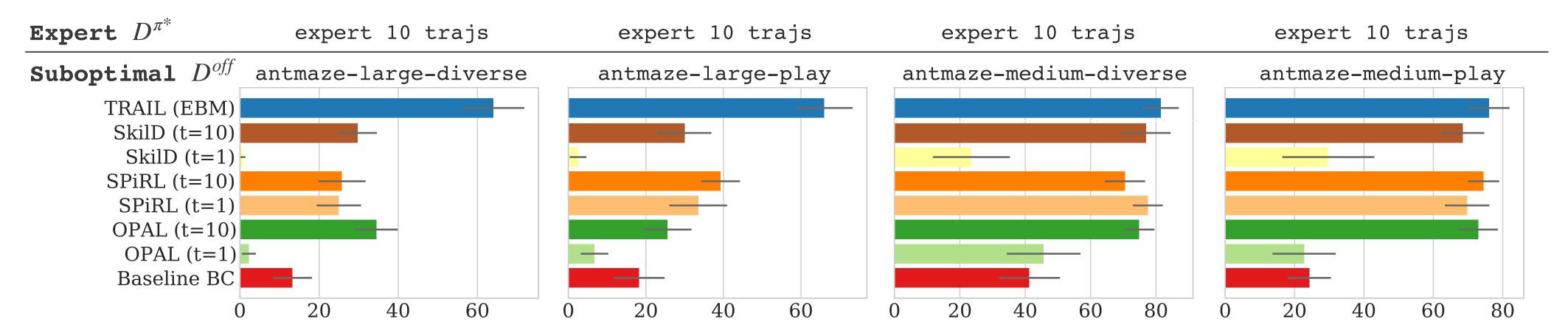
TRAIL EBM:
$$\mathcal{T}_Z(s'|s,\phi(s,a)) \propto \rho(s') \exp(-\|\phi(s,a)-\psi(s')\|^2)$$
.
$$\mathbb{E}_{d^{\mathrm{off}}}[-\log \mathcal{T}_Z(s'|s,\phi(s,a)))] = \mathrm{const}(d^{\mathrm{off}}) + \frac{1}{2}\mathbb{E}_{d^{\mathrm{off}}}[\|\phi(s,a)-\psi(s')\|^2] \quad \text{contrastive learning} \\ + \log \mathbb{E}_{\tilde{s}'\sim \rho}[\exp\{-\frac{1}{2}\|\phi(s,a)-\psi(\tilde{s}')\|^2\}]$$

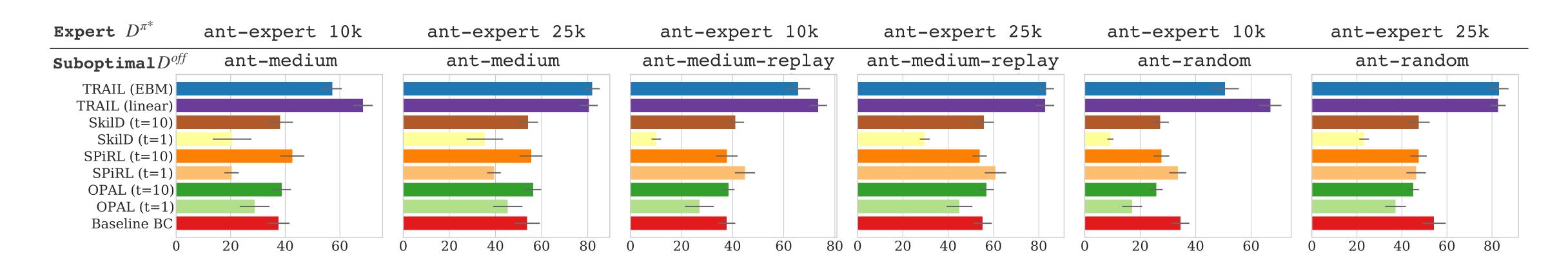
TRAIL linear:
$$\overline{\mathcal{T}}(s'|s,a) \propto \rho(s') \exp\{-||f(s,a)-g(s')||^2/2\} \propto \overline{\psi}(s')^\top \overline{\phi}(s,a)$$
 recover $\overline{\phi}$ with random Fourier features: $\overline{\phi}(s,a) = \cos(Wf(s,a)+b)$

 π_{α} and π_{Z} are neural-network parametrized Guassian policies.

Experiments





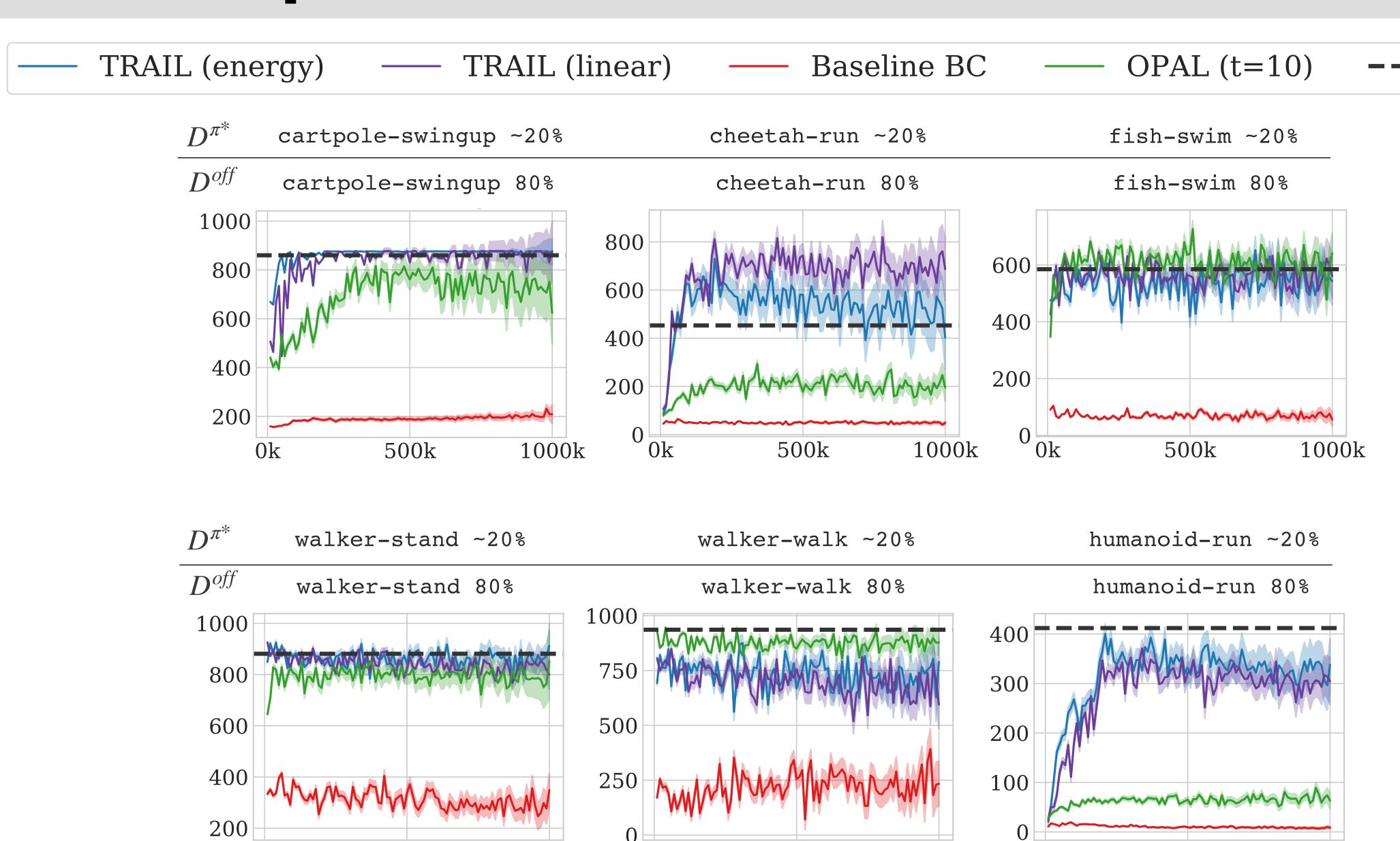


Experiments - DM Control Suite

CRR

1000k

500k



0k

1000k

1000k

0k

500k

0k

500k

Recap & Conclusion

- How to utilize additional offline data for imitation learning?
 - Learn action representations.
- What if the offline data is highly suboptimal or unimodal?
 - Learn transition model as opposed to temporal skills.
- Representation learning + imitation learning as an alternative to offline RL?
 - Beneficial especially in the absence of reward labels.

Thank you. Checkout

Paper: https://openreview.net/pdf?id=6q_2b6u0BnJ

Code: https://github.com/google-research/google-research/google-research/tree/master/rl_repr