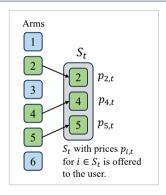
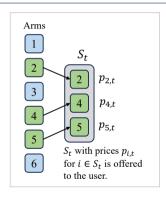
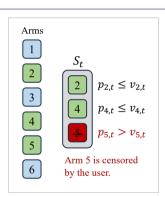
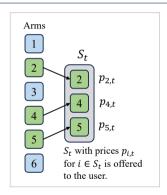
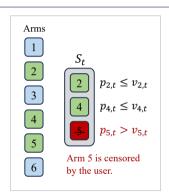
Jung-hun Kim, Min-hwan Oh Seoul National University

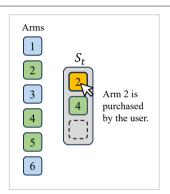


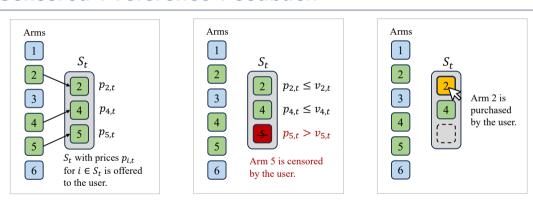












Motivating examples for this framework include

 e-commerce, hotel reservations, and air travel involving multiple products selection and pricing.

Purchase Model for Buyers

Definition 1 (Censored multinomial logit choice model)

Then, given S_t and p_t , the user purchases an arm $i \in S_t$ by paying $p_{i,t}$ according to the probability defined as follows:

$$\mathbb{P}_t(i|S_t, p_t) := \frac{\exp(v_{i,t} - \alpha_{i,t}p_{i,t})\mathbb{1}(p_{i,t} \leq v_{i,t})}{1 + \sum_{j \in S_t} \exp(v_{j,t} - \alpha_{j,t}p_{j,t})\mathbb{1}(p_{j,t} \leq v_{j,t})},$$
(1)

where $v_{i,t}$ is the latent valuation for the buyer and $\alpha_{i,t}$ is the latent price sensitivity parameter of item i.

The expected revenue from purchased arm $i \in S_t$ is represented as $R_{i,t}(S_t) = p_{i,t} \mathbb{P}_t(i|S_t, p_t)$. Then, the overall expected revenue is formulated as

$$R_t(S_t, p_t) = \sum_{i \in S_t} R_{i,t}(S_t).$$

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- We develop two algorithms that combine LCB pricing with Upper Confidence Bound (UCB) or Thompson Sampling (TS) for assortment selection, achieving regret bounds of $\widetilde{O}(d^{\frac{3}{2}}\sqrt{T/\kappa})$ and $\widetilde{O}(d^2\sqrt{T/\kappa})$, respectively.

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- We validate the effectiveness of our algorithms using synthetic datasets.

Thank You