

Everything, Everywhere, All at Once: Is Mechanistic Interpretability Identifiable?

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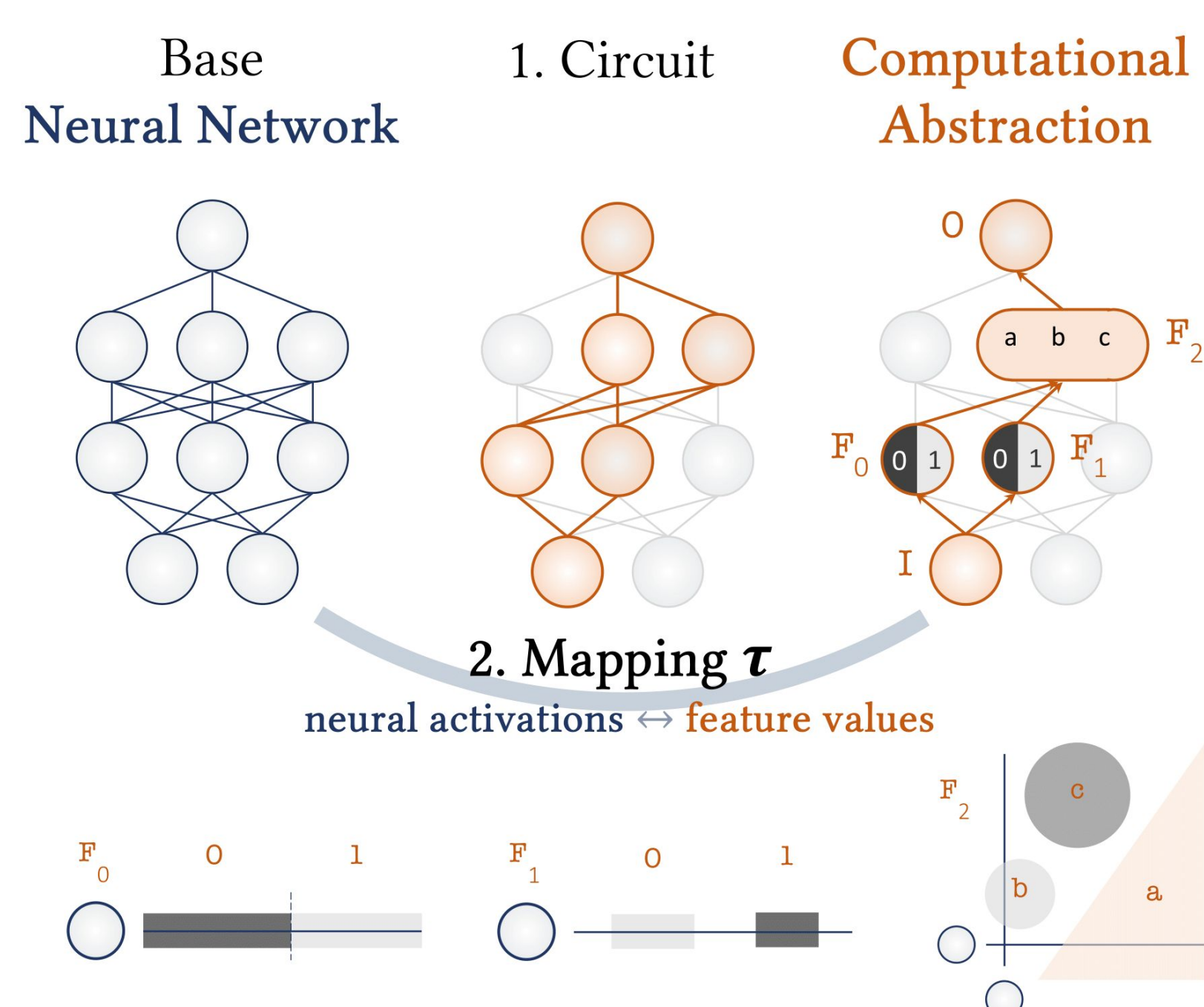
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What is Mechanistic Interpretability?

Mechanistic Interpretability (MI): reverse-engineer neural systems to uncover **simple, human-interpretable algorithms** embedded in the neural network structure.

MI explanations (**computational abstractions**) have two parts:

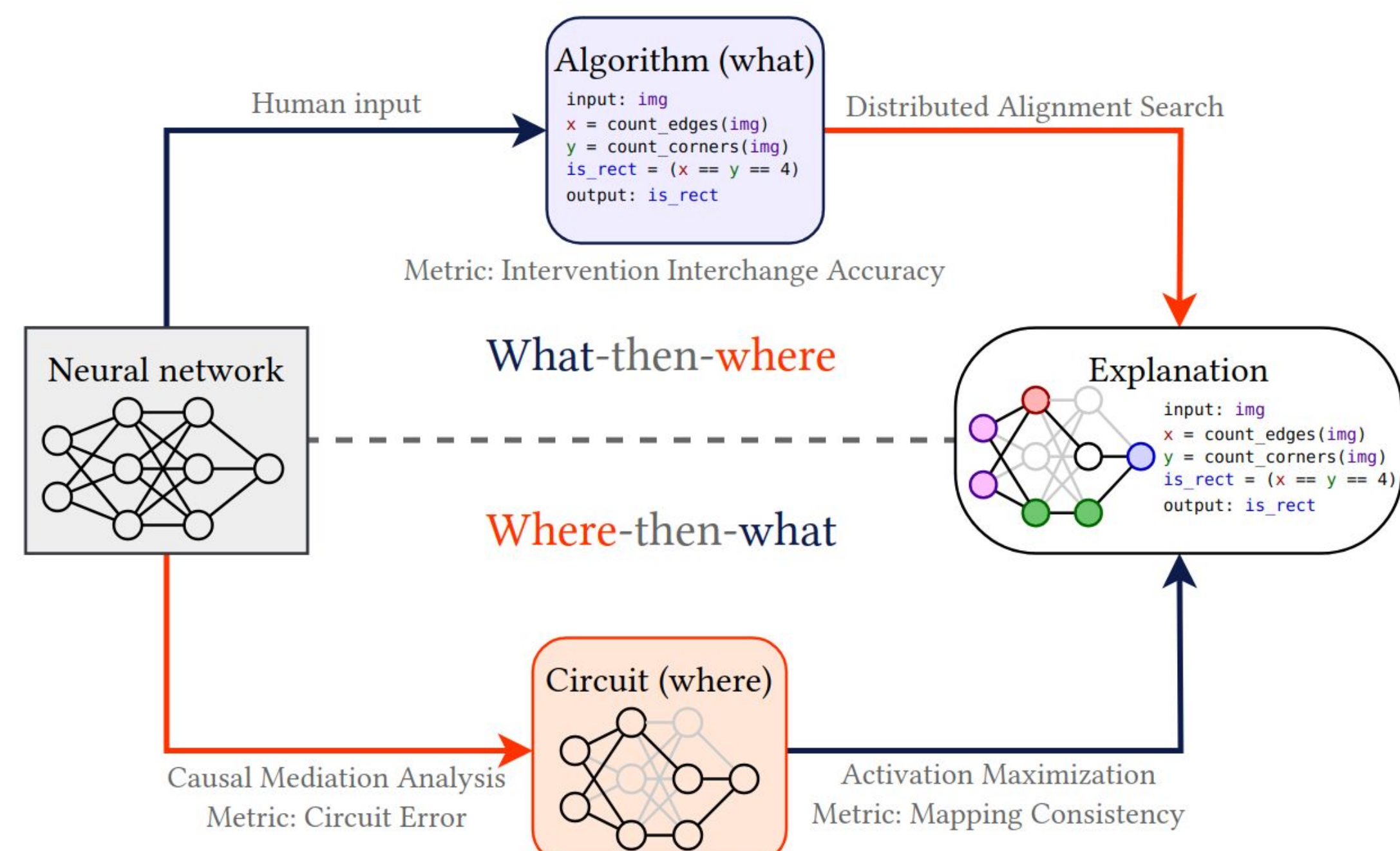
- **What** algorithm explains a given behavior? (**mapping** of low-level activations to high-level feature values)
- **Where** is the algorithm embedded in the network? (**circuit**: subset of the computational graph)



MI strategies and criteria

Current techniques can be classified into two strategies:

where-then-what and **what-then-where**.

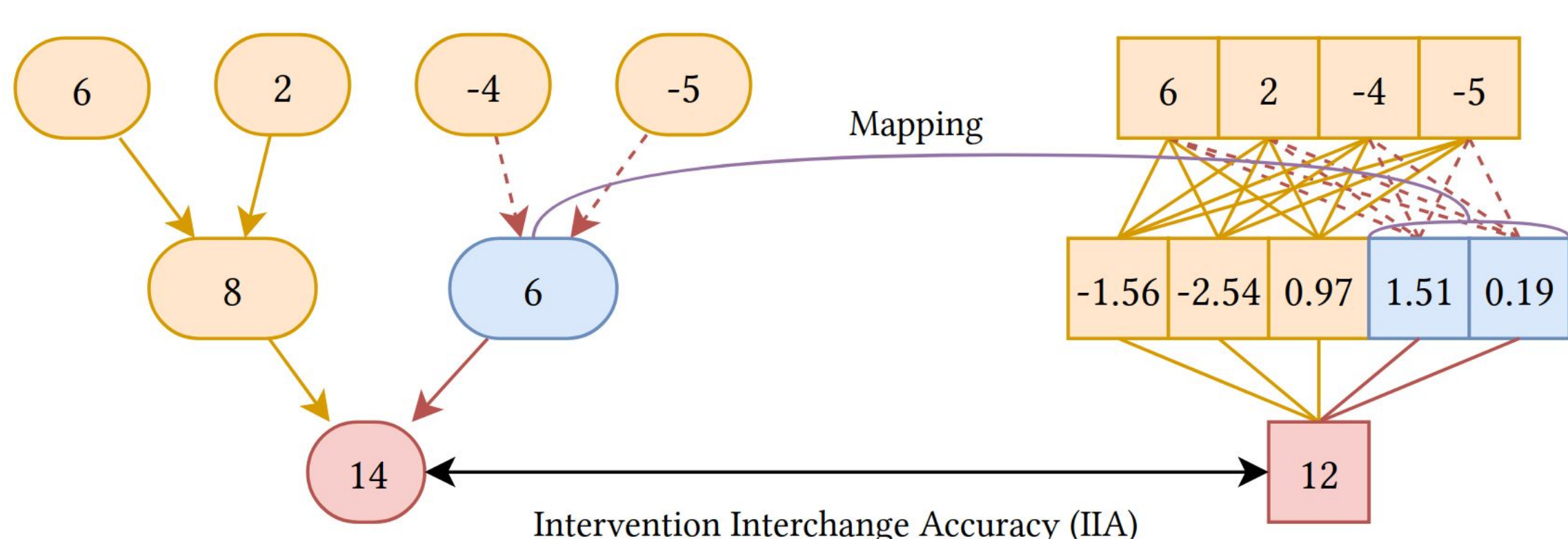


Where-then-what metrics:

- **Circuit error**: how well does the circuit replicate the behavior?
- **Mapping consistency**: does the mapping consistently align the computations in the low-level model with those in the high-level algorithm?

What-then-where metric:

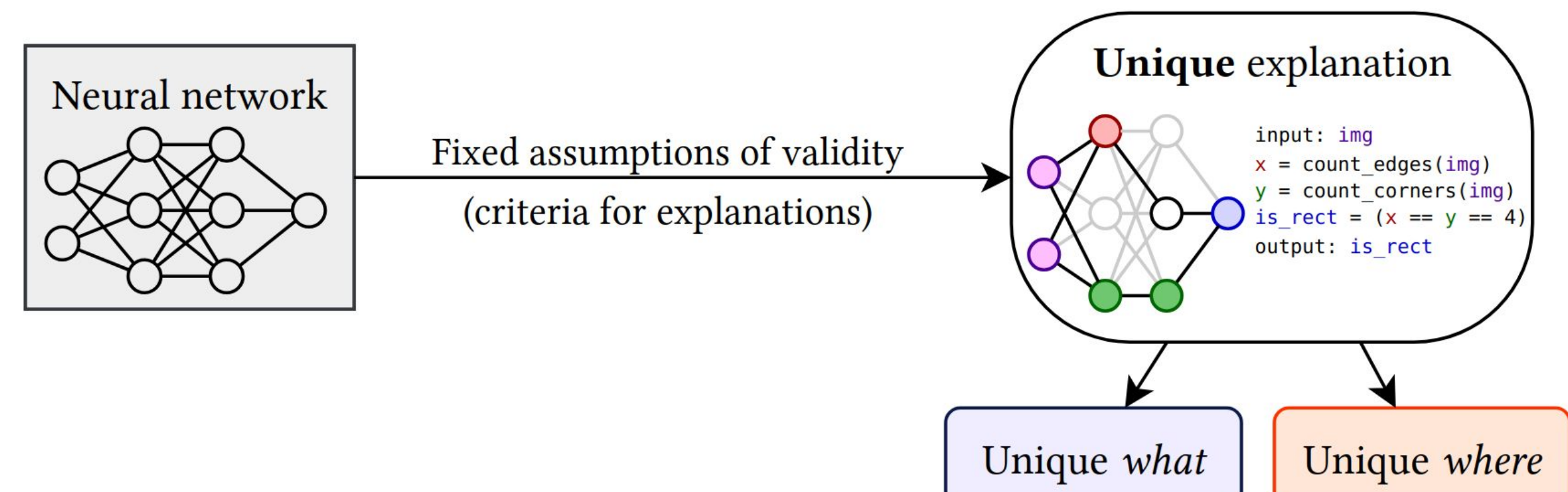
Intervention Interchange Accuracy (IIA)¹, measures the **causal alignment** of a (mapping, algorithm) pair, by performing **counterfactual interventions** on the variables of the high-level algorithm and those of the model through the mapping.



¹ Geiger, Atticus; Zhengxuan Wu; Hanson Lu; Josh Rozner; Elisa Kreiss; Thomas Icard; Noah D. Goodman; and Christopher Potts. 2022. *Inducing causal structure for interpretable neural networks*. In Proceedings of ICLR.

Research question

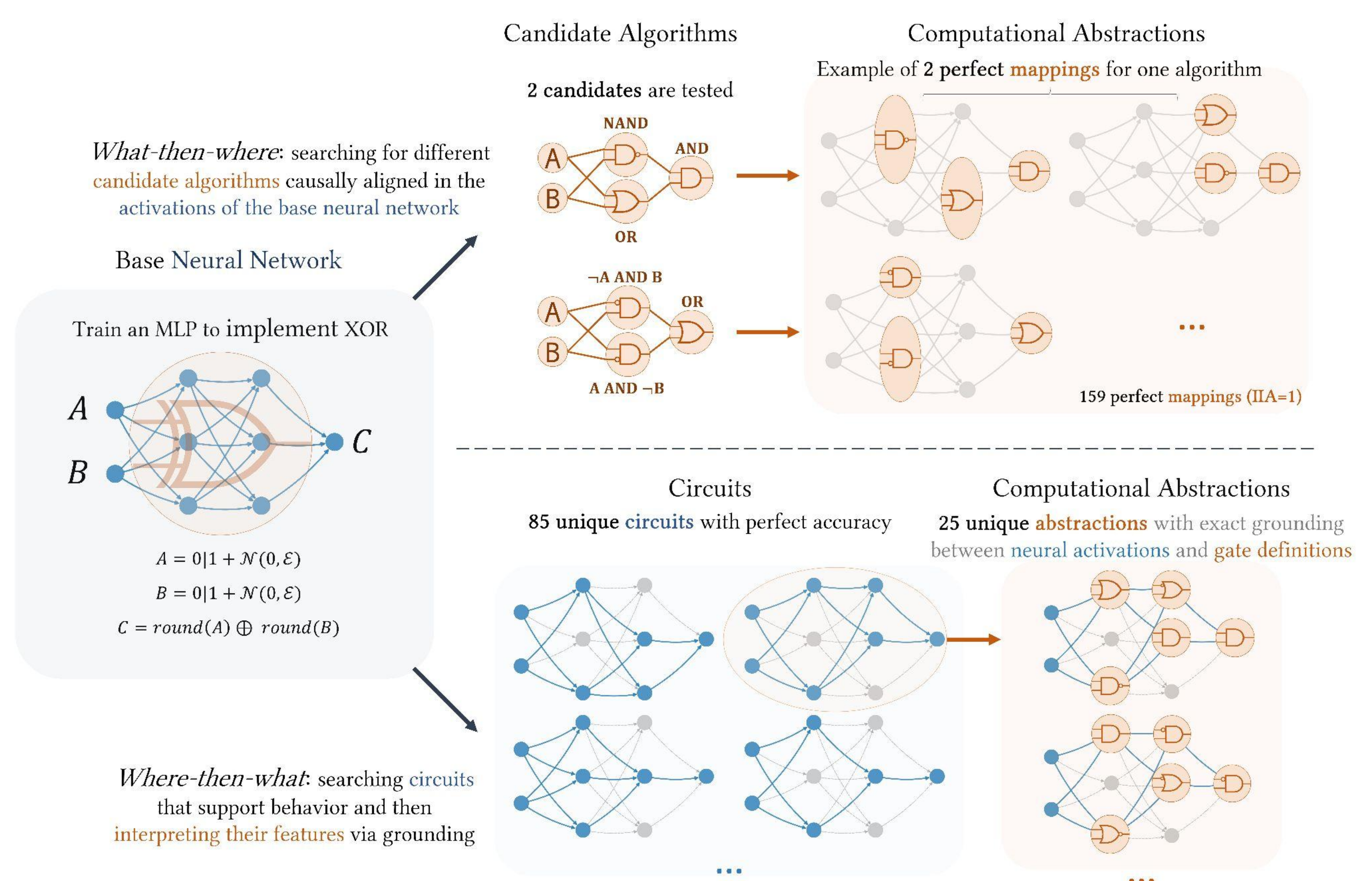
We ask whether MI is **identifiable**, borrowing this concept from statistics: When using **fixed criteria** for explaining a model's behavior, is the explanation unique? Is the **where** unique? Is the **what** unique?



Setup and results

- We train miniature **multi-layer perceptrons** (MLPs) on **Boolean functions** (XOR).
- We search for Boolean circuit explanations:
 - **What** sequence of logic gates is implemented by the MLP?
 - **Where** in the network is each gate implemented?

We **exhaustively** enumerate candidate algorithms and mappings, and test them with existing criteria (circuit error and mapping consistency for **where-then-what**, and IIA for **what-then-where**).



Even with strict causal alignment methods, we find **multiple, incompatible explanations** of the same neural computation. We encounter identifiability failures at every stage:

The **what** is not unique → Given the **what**, the **where** is not unique

The **where** is not unique → Given the **where**, the **what** is not unique

Additionally, the problem does not disappear when increasing the size of the network or changing training dynamics (duration, noise, multi-task setting).

Discussion and future work

Where to go from here? We suggest possible paths forward:

Change the criteria: Refine validity criteria with stronger constraints (based on causal abstraction), or use multi-criteria validation for explanations.

Change the expectation: Depending on the pragmatic goals of interpretability, uniqueness may not be required for **predictability** or **controllability**. However, if interpretability is expected to provide **understanding**, then non-identifiability becomes a problem.

Fundamental limits? In some scientific domains, multiple valid theories coexist; MI may similarly be underdetermined, and uniqueness might be unachievable without additional constraints.