

Learning from Negative Feedback, or Positive Feedback or Both

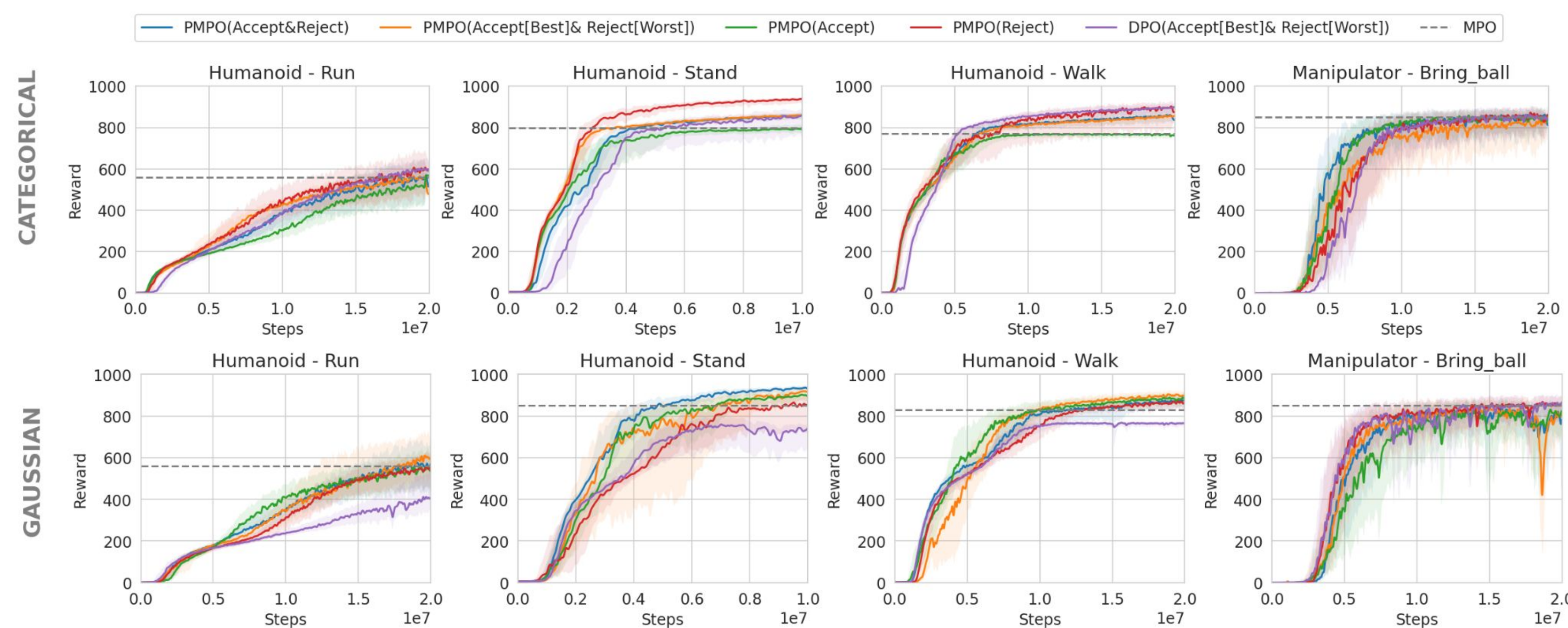
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Introduction

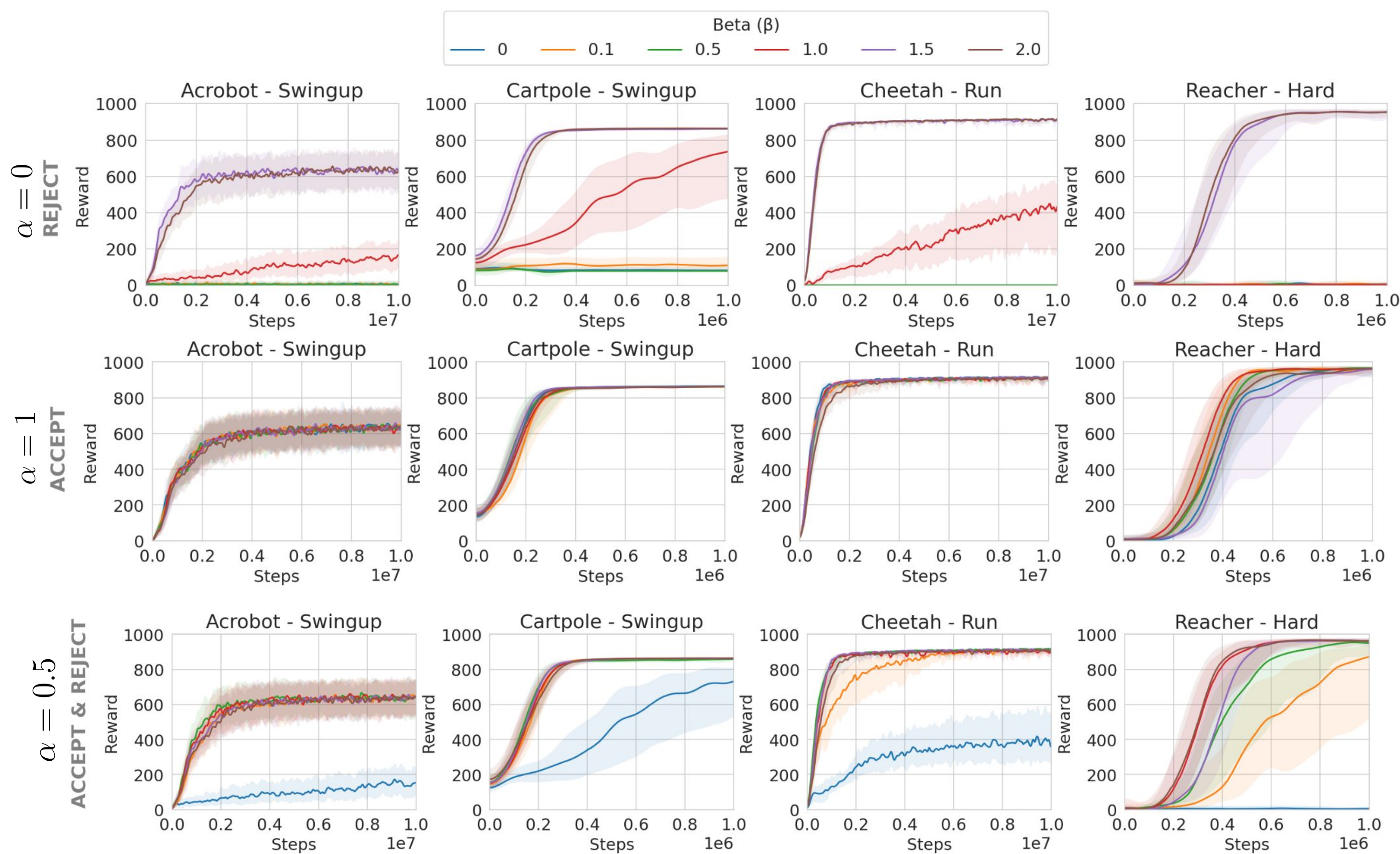
- Existing preference optimization methods often require paired feedback (positive vs. negative).
- This limits their use when only unpaired feedback (e.g., only positive or only negative) is available.
- We introduce **PMPO**, a novel approach decoupling learning from positive and negative feedback.
- This allows learning even when only one feedback type is present, including stable learning from *negative feedback alone*

Control tasks experiments

Sample 4 generations and rank them according to the Q function. Label the top 2 with positive feedback and the bottom 2 with negative feedback.



Ablation of alpha and beta parameters



PMPO Policy Improvement Objective

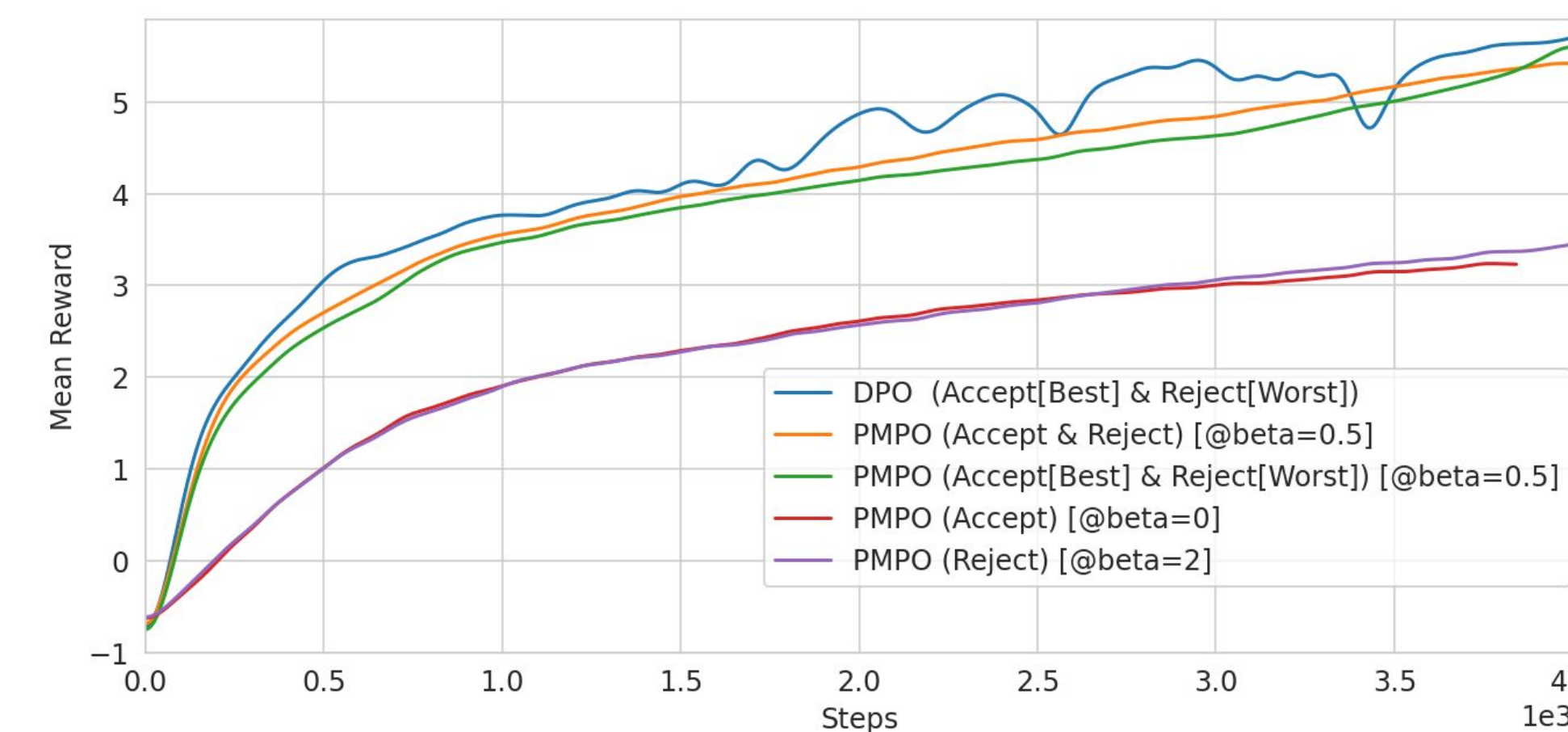
Policy improvement update rule for Improving over the current reference policy using the labeled positive/negative feedback samples:

$$\mathcal{J}(\pi_{\theta}; x) = \alpha \underbrace{\mathbb{E}_{y \sim \mathcal{D}_a} [\log \pi_{\theta}(y|x)]}_{\text{Learn from Positive Feedback}} - (1-\alpha) \underbrace{\mathbb{E}_{y \sim \mathcal{D}_r} [\log \pi_{\theta}(y|x)] - \beta \text{KL}(\pi_{\text{ref}} \parallel \pi_{\theta}; x)}_{\text{Learn from Negative Feedback}}$$

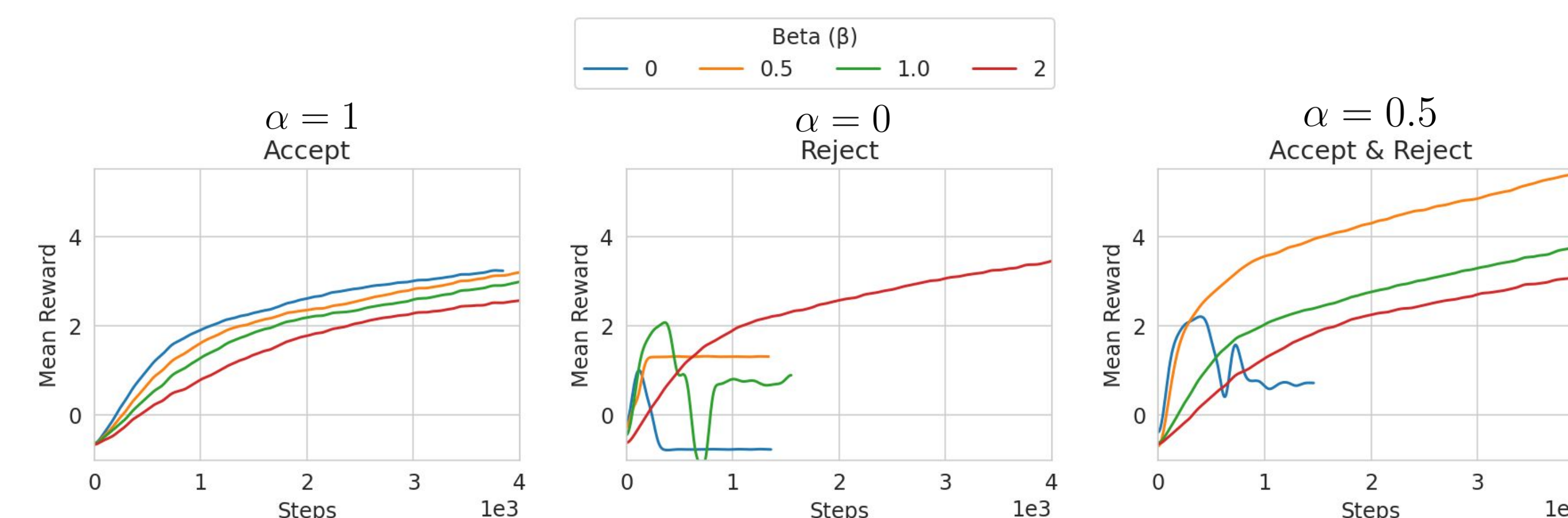
- x : Input context/conditioning variable (e.g., state, prompt).
- π_{θ} : Policy being optimized.
- π_{ref} : Reference policy (samples y are drawn from this).
- \mathcal{D}_a : Dataset providing positive ("accepted") feedback ([Blue Term](#)).
- \mathcal{D}_r : Dataset providing negative ("rejected") feedback ([Red Term](#)).
- α : Controls trade-off between positive ($\alpha \rightarrow 1$) and negative ($\alpha \rightarrow 0$) feedback objectives.
- β : Strength of KL regularization (essential when learning from negative feedback, i.e. when $\alpha < 1$).

RLHF Experiments with Gemma 2B

Sample 4 generations and rank them according to the learned reward function. Label the top 2 with positive feedback and bottom 2 with negative feedback.



Ablation of alpha and beta parameters



Policy Optimization as Probabilistic Inference

Objective: Find a policy that maximizes the expected likelihood of generations with positive feedback, i.e.,

$$\max_{\theta} \mathbb{E}_{y \sim \pi_{\theta}(y|x)} [p(\mathbf{S} = 1|y, x)]$$

- $p(\mathbf{S} = 1|y, x)$: Likelihood that output y receives positive feedback
- $p(\mathbf{S} = 0|y, x)$: Likelihood that output y receives negative feedback

- Note: these likelihoods sum to one: $p(\mathbf{S} = 1|y, x) + p(\mathbf{S} = 0|y, x) = 1$

Learning from positive feedback

Using Expectation-Maximization (EM), we obtain a one-step policy improvement over the current estimate:

$$\pi_{\text{new}}(y|x) = \arg \max_{\theta} \mathbb{E}_{y \sim q(y|x)} [\log \pi_{\theta}(y|x)]$$

Where

$$\underbrace{q(y|x)}_{\text{Posterior}} \propto \underbrace{\pi_{\text{ref}}(y|x)}_{\text{Prior}} \underbrace{p(\mathbf{S} = 1|y, x)}_{\text{Likelihood Function}}$$

If for y with positive feedback we choose $p(\mathbf{S} = 1|y, x) = 1$, we get the [update rule in blue](#).

Learning from negative feedback

Applying reparameterization $p(\mathbf{S} = 1|y, x) = 1 - p(\mathbf{S} = 0|y, x)$ gives the update rule based on likelihood of negative feedback:

$$\pi_{\text{new}}(y|x) = \arg \max_{\theta} [-\mathbb{E}_{y \sim t(y|x)} [\log \pi_{\theta}(y|x)] - \beta \text{KL}(\pi_{\text{ref}} \parallel \pi_{\theta}; x)]$$

Where

$$\underbrace{t(y|x)}_{\text{Posterior}} \propto \underbrace{\pi_{\text{ref}}(y|x)}_{\text{Prior}} \underbrace{p(\mathbf{S} = 0|y, x)}_{\text{Likelihood Function}}$$

If for y with negative feedback we choose $p(\mathbf{S} = 0|y, x) = 1$ we get the [update rule in red](#).

Note: When only learning from negative feedback, derivations suggests $\beta \geq 1$ is required for effective learning:

$$\beta = \frac{1}{\int \pi_{\text{ref}}(y|x) p(\mathbf{S} = 0|y, x) dy}$$

Conclusion

- PMPO provides a flexible, intuitive, and theoretically grounded algorithm for policy optimization.
- Successfully extends learning to utilize unpaired, unbalanced, positive-only, and crucially, **negative-only** feedback. Addresses limitations of existing methods requiring paired data.
- Limitation:** Effective negative learning benefits from accurate KL estimation.